

Intersymbol Interference:

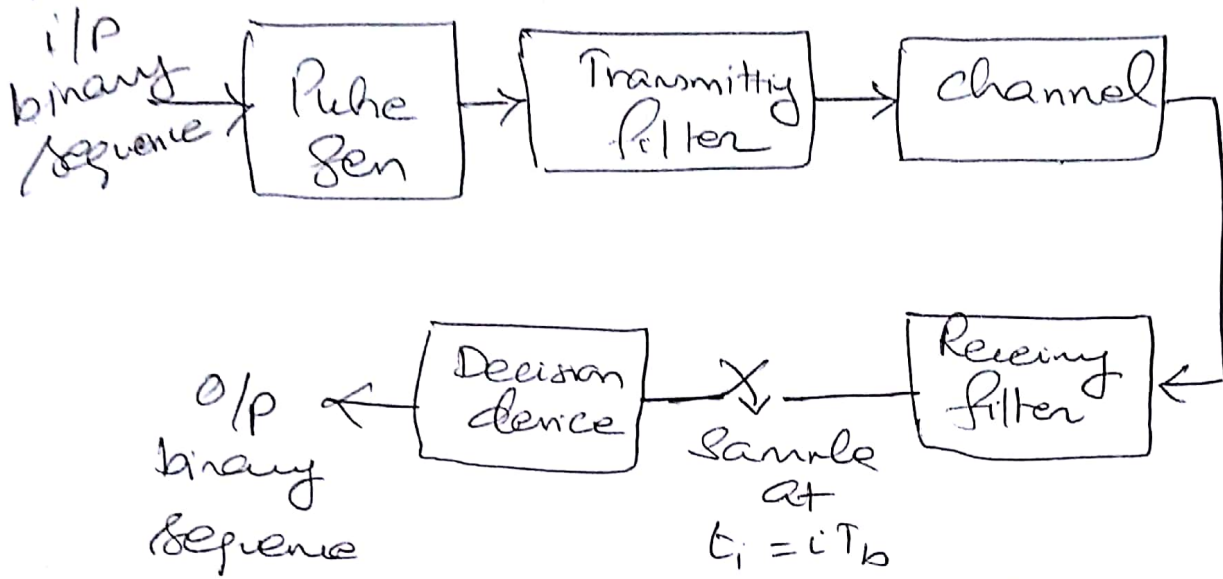
When a short pulse of duration T_b sec is transmitted through a bandlimited system, the frequency components of the input pulse are differentially attenuated and hence differentially delayed by the system.

Consequently the pulse appearing at the o/p of the system is dispersed over an interval longer than T_b sec and interfere with each other.

The overlapping of pulses is referred as intersymbol interference (ISI). ISI arises due to imperfections in the overall frequency response of the system.

The presence of ISI increases the error in the decision device at the receiver o/p.

Baseband binary PAM System



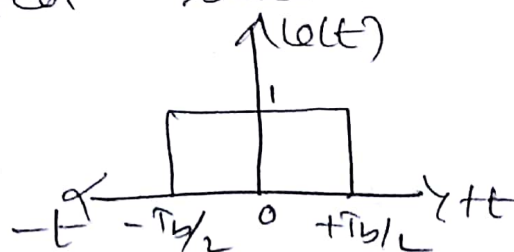
The i/p consists of a binary data sequence $\{b_k\}$ with a bit duration of T_b secs.

This sequence is applied to a pulse generator, producing the discrete PAM signal

Given by

$$x(t) = \sum_{k=-\infty}^{+\infty} a_k u(t - kT_b) \quad \text{--- (1)}$$

where $u(t)$ denotes the basic rectangular pulse normalized such that $u(0) = 1$

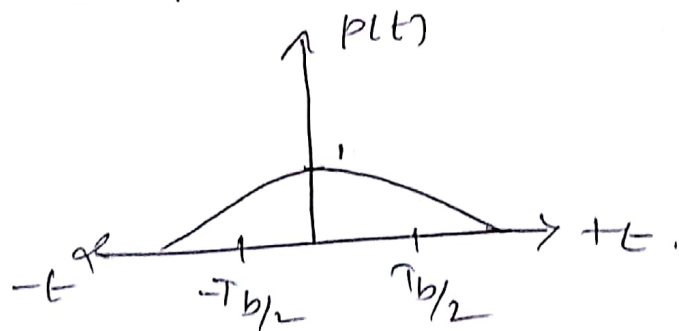


coefficient a_k depends on the o/p data and type of format used

Signal $x(t)$ passes through a transmitting filter $H_T(f)$. The resulting filter o/p is the transmitted signal which is modified as a result of transmission through the channel of transfer function $H_C(f)$. The channel may be coaxial cable or optical fiber where the major source of degradation is dispersion. The spreading of pulse is called dispersion. The channel o/p is passed through a receiving filter of transfer function $H_R(f)$. The filter o/p is sampled periodically. When the sample value ~~is~~ exceeds the threshold value, the

Decision is made in favor of symbol 1 & if the sample value is less than the threshold, then the decision is made in favor of symbol 0. If the sample value is equal to the threshold value exactly, then the decision is made in favor of sym-0 & sym-1.

Let $P(t)$ be the received pulse shape such that $P(0)=1$



Then the received signal is given by

$$y(t) = \mu \sum_{k=-\infty}^{\infty} a_k P(t - kT_b) \quad \text{--- (2)}$$

μ - scaling factor depends on the channel

The o/p from the sample is given by

$$y(t_i) = \mu \sum_{k=-\infty}^{+\infty} a_k P(\epsilon_i - kT_b)$$

$$= \mu \sum_{k=-\infty}^{+\infty} a_k P(iT_b - kT_b) \rightarrow \textcircled{3}$$

Sub. $i = k$, in $\textcircled{3}$ we get

$$y(t_i) = \mu a_i P(0) + \mu \sum_{\substack{k=-\infty \\ k \neq i}}^{+\infty} P(iT_b - kT_b)$$

When $P(0) = 1$, then

$$y(t_i) = \mu a_i + \mu \sum_{\substack{k=-\infty \\ k \neq i}}^{+\infty} P(iT_b - kT_b) \rightarrow \textcircled{4}$$

$y(t_i) = \mu a_i$ implies zero ISI
 And this is the sample value produced by the i^{th} transmitted bit. The second term is due to the residual effect of all other transmitted bits on the decoding of the i^{th} transmitted bit.

∴ The condition for the (45)
~~perfect reception~~ perfect reception
 in the absence of noise is
 given by

$$P(cT_b - kT_b) = \begin{cases} 1 & c = k \\ 0 & c \neq k \end{cases} \quad (5)$$

This condition is referred as
 Nyquist criterion for distortionless
 baseband binary transmission.

Let us consider a sequence
 of samples $\{p(nT_b)\}$ where

$$n = 0, \pm 1, \pm 2, \pm 3, \dots$$

$\dots \quad \begin{array}{cccccccc} | & | & | & | & | & | & | & | \\ \hline & -3 & -2 & -1 & 0 & 1 & 2 & 3 \dots \end{array}$

According to sampling theorem

sampling in the time domain

produces periodicity in the

frequency domain

$$T_s = T_b$$

$$\therefore P_f(f) = R_b \sum_{n=-\infty}^{+\infty} P(f - nR_b) \quad (6)$$

where $R_b = 1/T_b$

where $P_g(t)$ is the Fourier transform of an infinite periodic sequence of delta function of period T_b whose strengths are weighted by the respective samples of $p(t)$ given by

$$\sum_{m=-\infty}^{+\infty} p(mT_b) \delta(t - mT_b)$$

Taking Fourier transform

we get

$$P_g(f) = \int_{-\infty}^{+\infty} \left(\sum_{m=-\infty}^{+\infty} p(mT_b) \delta(t - mT_b) \right) e^{-j\omega t} dt \rightarrow (7)$$

In order to inverse the condition for zero ISI,

Replace m by $i-k$ in (5)

we get

$$p(mT_b) = \begin{cases} 1 & m=0 \\ 0 & m \neq 0 \end{cases} \rightarrow (8)$$

Sub. $m = 0$ we get

(46)

$$\begin{aligned} P_f(f) &= \int_{-\infty}^{+\infty} P(0) f(t) e^{-j\omega t} dt \\ &= P(0) \int_{-\infty}^{+\infty} f(t) e^{-j\omega t} dt \\ &= 1 \rightarrow \textcircled{8} \end{aligned}$$

Equation eq. (6) & (9) we get

$$R_b \sum_{n=-\infty}^{+\infty} P(f - nR_b) = 1$$

$$\sum_{n=-\infty}^{+\infty} P(f - nR_b) = \frac{1}{R_b} = T_b$$

$\rightarrow \textcircled{10}$

This is the requirement for zero ISI in the frequency domain.

Ideal solution:

- narrowest band is obtained by permitting only one non-zero components in eq. (10)
- f lies within the band
- $-R_b/2$ to $+R_b/2$.

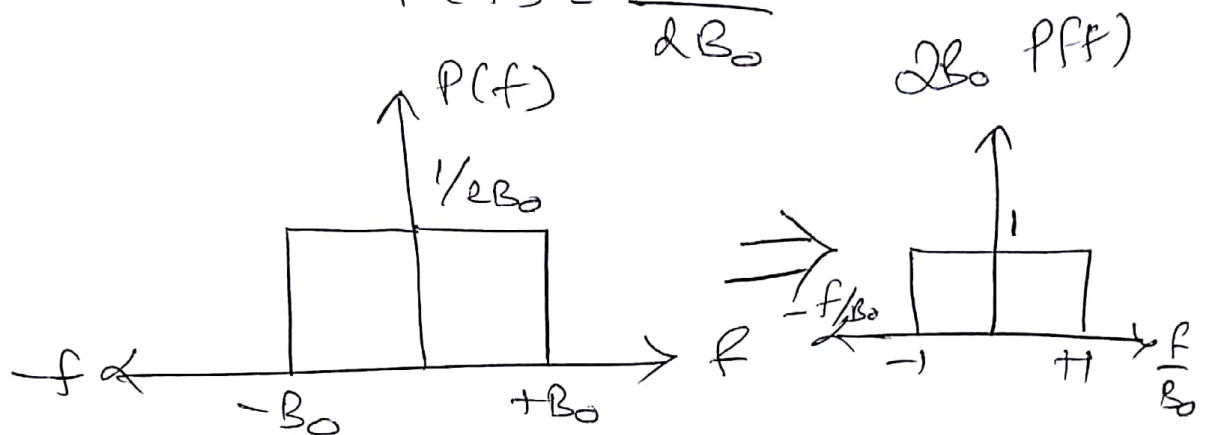
Ideal Solution:

Let $B_0 = R_b/2$, then

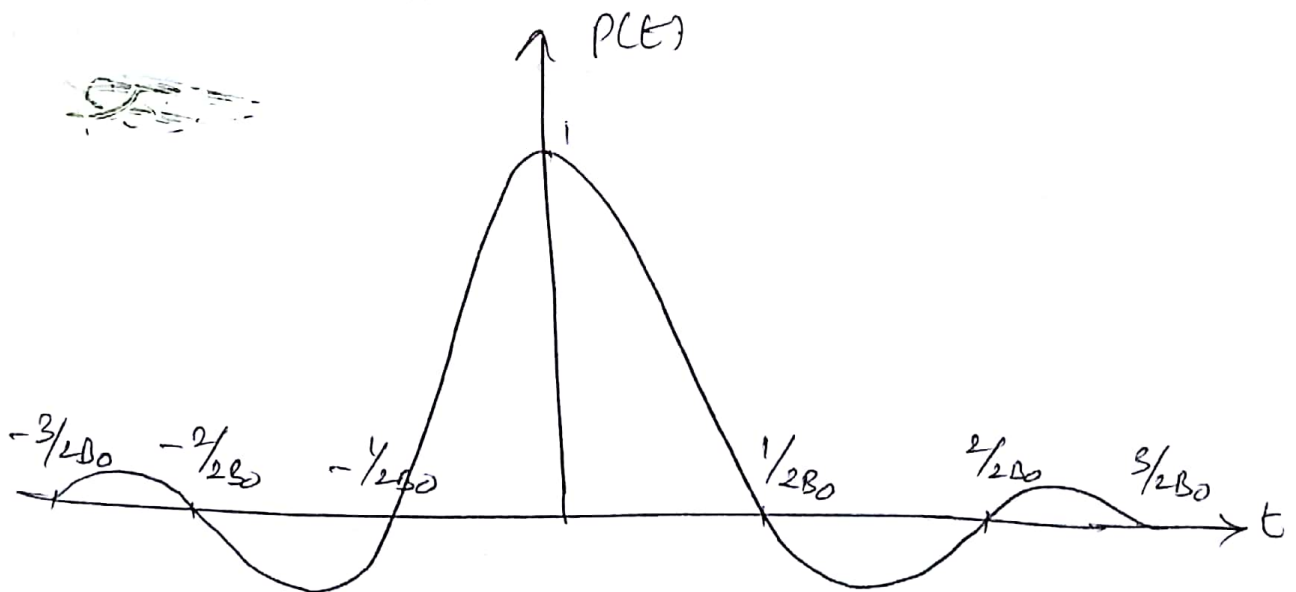
Eq (10) can be written as

$$\sum_{n=-\infty}^{+\infty} P(f - n 2B_0) = \frac{1}{2B_0}$$

When $n=0$, $P(f) = \frac{1}{2B_0}$



$$P(f) = \frac{1}{2B_0} \text{srect} \left(\frac{f}{2B_0} \right)$$



\Rightarrow Minimum Bandwidth
 $B = B_0 = R_b/2$

Advantages of Sinc Pulse:

Requires min. Bandwidth

$$B = B_0 = B_b/2 = \frac{1}{2T_b}$$

Disadvantages:

1. The amplitude characteristics of $P(f)$ should be flat from $-B_0$ to B_0 and zero elsewhere. This is not physically realizable.
2. Slow rate of decay of the sine pulse till infinity.

Raised Cosine Spectrum:

- Extending the bandwidth from B_0 to a value between B_0 and $2B_0$.
- 3 components are permitted in the series

$$P(f) + P(f - 2B_0) + P(f + 2B_0) = \frac{1}{2B_0}$$

$$-B_0 \leq f \leq B_0$$

- $P(f)$ is said to be the raised cosine spectrum.
- Frequency characteristics of raised cosine spectrum has a flat portion and a roll-off portion that has a sinusoidal form.

$$P(f) = \begin{cases} \frac{1}{2B_0} & |f| < f_1 \\ \frac{1}{4B_0} \left\{ 1 + \cos \left[\frac{\pi (|f| - f_1)}{2B_0 - 2f_1} \right] \right\} & f_1 \leq |f| < 2B_0 - f_1 \\ 0 & |f| \geq 2B_0 - f_1 \end{cases}$$

Frequency f_1 and bandwidth B_0 are related by

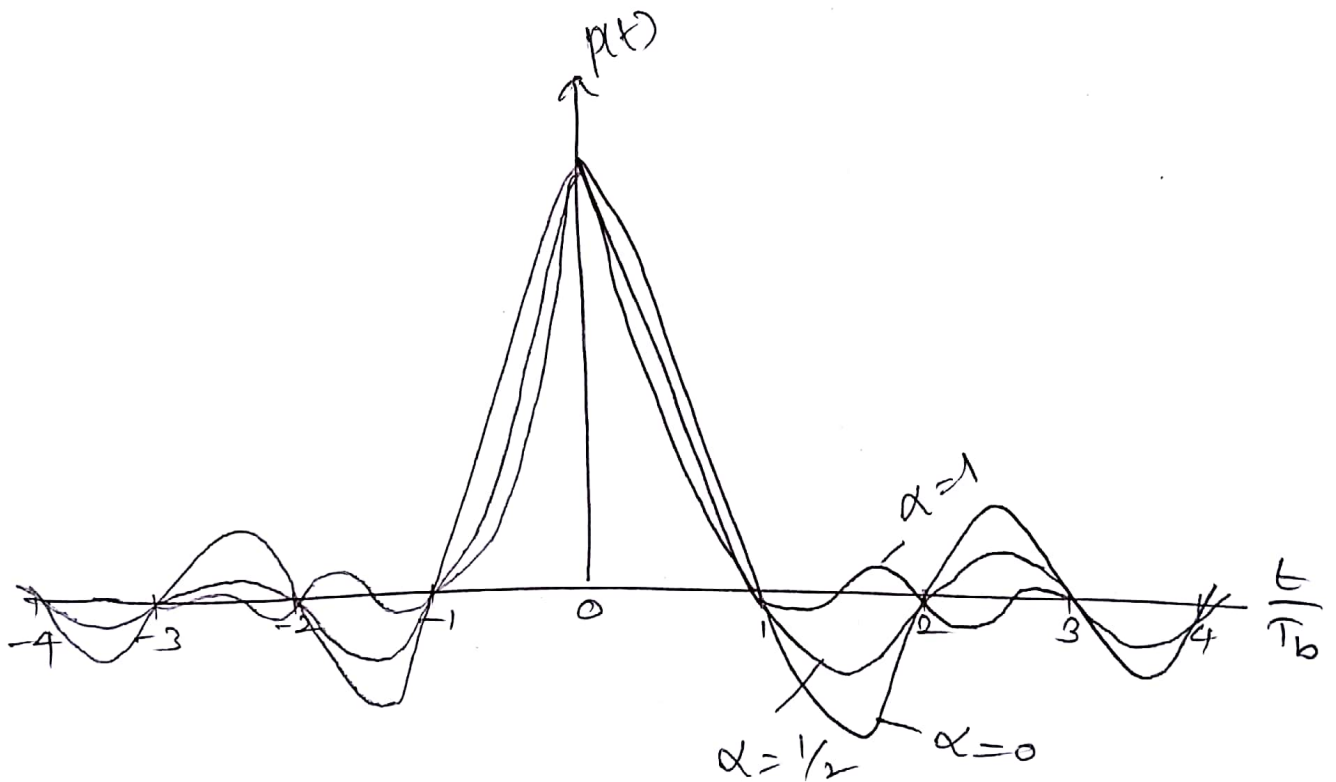
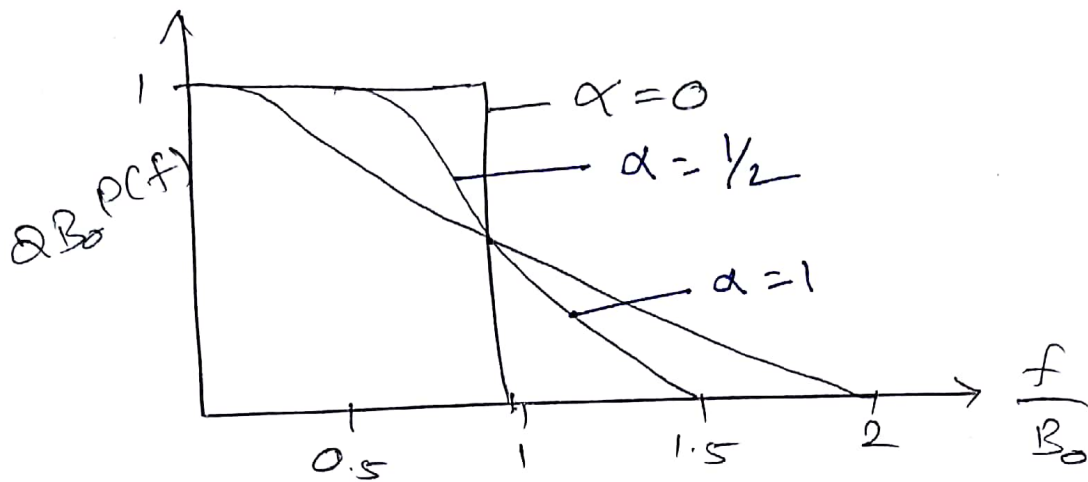
$$\alpha = 1 - \frac{f_1}{B_0}$$

α - Roll-off factor

when $\alpha = 0$, $f_1 = B_0 \Rightarrow$ Min. Bandwidth solution.

Normalized $P(f)$

(48)



Inverse fourier transform $P(t)$ is given by

$$P(t) = \text{Sinc}(2B_0 t) \cdot \frac{\cos(2\pi\alpha B_0 t)}{1 - 16\alpha^2 B_0^2 t^2}$$

$\text{Sinc}(2B_0 t) \rightarrow$ associated with ideal LPF.

$\frac{1}{|t|^2} \rightarrow$ Reduces the tails of the pulse considerably below that obtained from the ideal LPF.

- When α increases from 0 to unity, the amount of ISI decreases.
- Zero crossings at $t = \pm 3T_b/2, \pm 5T_b/2$, in addition to usual zero crossings at the sampling instants $t = \pm T_b, \pm 2T_b, \dots$

$$\text{Bandwidth } B = 2B_0 - f_1$$

$$\text{where } f_1 = B_0(1 - \alpha)$$

Correlative coding:

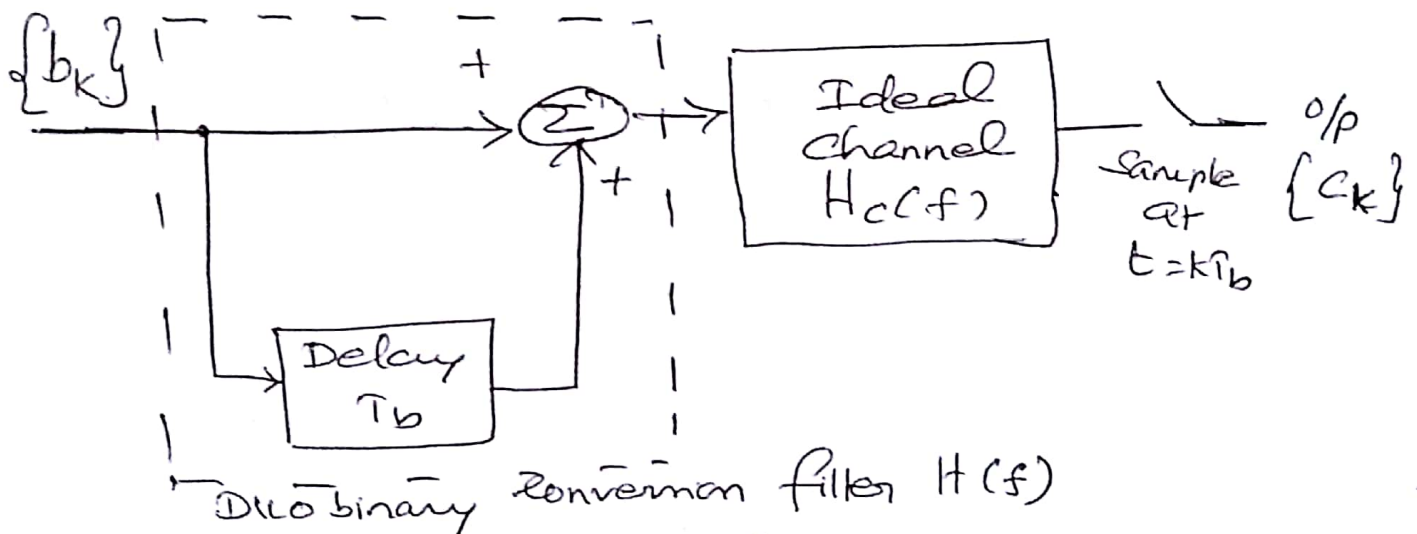
- Practical means of achieving the theoretical maximum signalling rate of $2B_0$ bits/sec in a bandwidth of B_0 Hz is called

(49)

Correlative coding Duo binary Signalling:

- Duo implies doubling the transmission capacity of a straight binary system.

Duo binary Signalling Scheme.



$b_k \rightarrow$ i/p binary sequence

Let b_k be the i/p binary sequence consists of uncorrelated binary digits each having a duration of T_b sec and represented in Polar format as

Sym - 1	-	+1V
Sym - 0	-	-1V

When this sequence is applied to duobinary convolution filter it is converted into a three level o/p namely $-2, 0$ & $+2V$

Sequence is passed through a simple filter consists of delay element.

For every unit impulse applied to the i/p of this filter, we get two unit impulses spaced at T_b sec. apart at the filter o/p.

The o/p from the duobinary convolution filter is given by

$$C_k = b_k + b_{k-1}$$

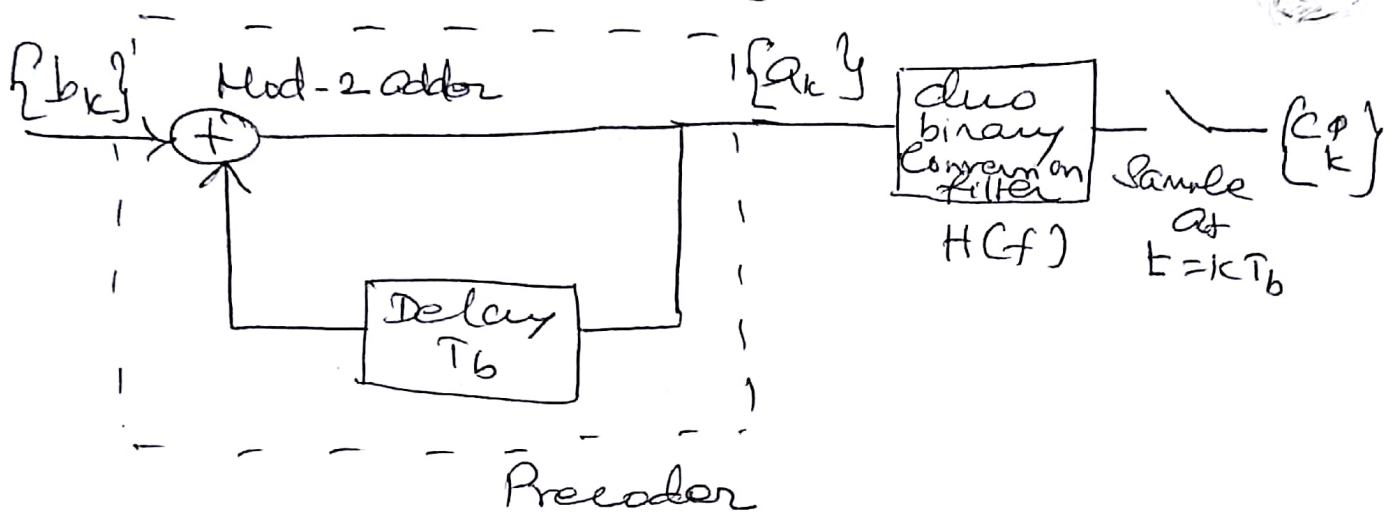
Then the o/p from the receiver is given by

$$b_k = C_k - b_{k-1}$$

Drawbacks:

If one bit is erroneous, the remaining bits become erroneous.

Pre-coded duobinary scheme:



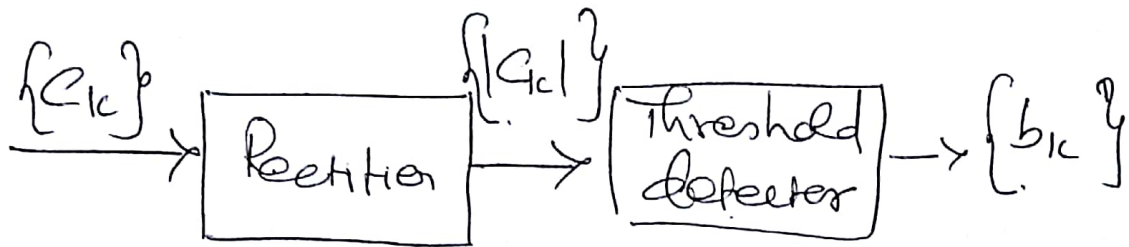
Let $\{b_k\}$ be the i/p to the Pre-coder and the o/p from the Pre-coder is given by

$$a_k = b_k \oplus a_{k-1} \quad \text{mod-2}$$

The resulting Pre-coder o/p $\{a_k\}$ is next applied to the duobinary coder. Then, the o/p from the duobinary coder is given by

$$c_k = a_k + a_{k-1} \quad \text{Polar form}$$

At the receiver side, the received sequence $\{c_k\}$ is applied to a differentiator followed by Threshold detector.

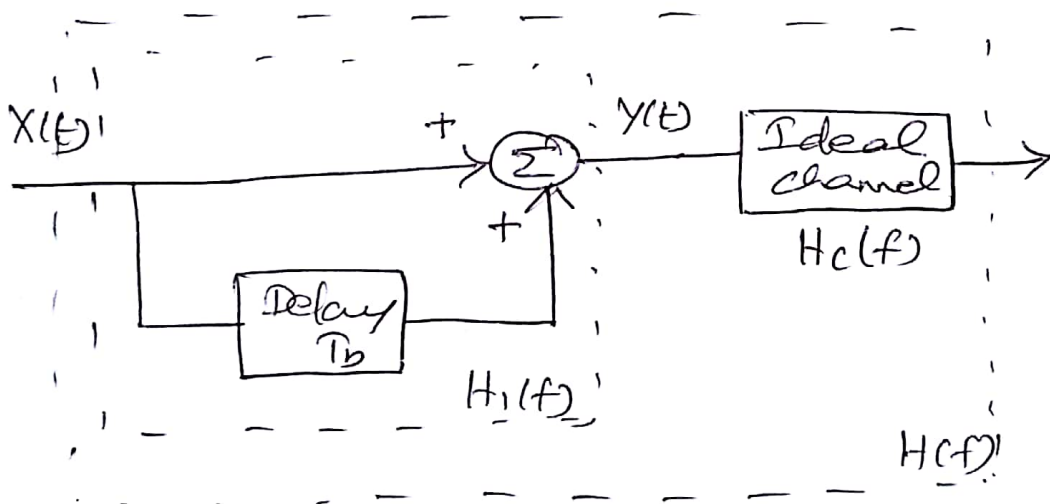


Decision rule:

$$c_k = \begin{cases} \pm 2 \text{ Volts} & \text{if } b_k \text{ represents Sym-0} \\ 0 \text{ Volt} & \text{if } b_k \text{ represents Sym-1} \end{cases}$$

$$b_k = \begin{cases} \text{Sym 0} & \text{if } |c_k| > 1 \text{ V} \\ \text{Sym 1} & \text{if } |c_k| < 1 \text{ V} \end{cases}$$

Impulse response of duobinary conversion filter:



The duobinary conversion filter consists of an ideal delay element. Let $X(t)$ be the input to the duobinary

conversion filter and the
o/p from the duobinary
conversion filter is given by

$$Y(t) = X(t) + X(t - T_b) \rightarrow (1)$$

Taking fourier transform of eq (1)
we get

$$\begin{aligned} Y(f) &= X(f) + X(f) e^{-j\omega T_b} \\ &= X(f) (1 + e^{-j\omega T_b}) \end{aligned}$$

$$\frac{Y(f)}{X(f)} = 1 + e^{-j\omega T_b} = H_1(f) \rightarrow (2)$$

where $H_1(f)$ be the transfer
function of the duobinary
conversion filter. and T_b be the
bit duration.

For an ideal channel of
bandwidth B_0 which is equal
to $R_b/2$, the transfer function
of the ideal channel is

Given by

$$H_c(f) = \begin{cases} 1 & |f| \leq R_b/2 \\ 0 & |f| > R_b/2 \end{cases} \rightarrow (3)$$

The overall transfer function of the system is given by

$$H(f) = H_1(f) \cdot H_2(f) \\ = (1 + e^{-j2\pi f T_b}) H_c(f) \rightarrow \textcircled{4}$$

Sub eq. $\textcircled{3}$ in $\textcircled{4}$ we get

$$H(f) = \begin{cases} 1 + e^{-j2\pi f T_b} & |f| \leq R_b/2 \\ 0 & \text{otherwise} \end{cases} \rightarrow \textcircled{5}$$

Impulse response can be obtained by taking the inverse Fourier transform of $H(f)$ as given

$$h(t) = \int_{-\infty}^{\infty} H(f) e^{+j2\pi f t} df \\ = \int_{-R_b/2}^{+R_b/2} (1 + e^{-j2\pi f T_b}) e^{+j2\pi f t} df \\ = \int_{-R_b/2}^{+R_b/2} e^{+j2\pi f t} df + \int_{-R_b/2}^{+R_b/2} e^{+j2\pi f (t - T_b)} df$$

$$\begin{aligned}
&= \left[\frac{e^{j2\pi ft}}{j2\pi t} \right]_{-R_b/2}^{+R_b/2} + \left[\frac{e^{j2\pi f(t-T_b)}}{j2\pi(t-T_b)} \right]_{-R_b/2}^{R_b/2} \\
&= \frac{e^{j\frac{\pi}{2} R_b t} - e^{-j\frac{\pi}{2} R_b t}}{j2\pi t} + \frac{e^{j\frac{\pi}{2} R_b (t-T_b)} - e^{-j\frac{\pi}{2} R_b (t-T_b)}}{j2\pi(t-T_b)} \\
&= \frac{\cancel{j2} \sin(\pi R_b t)}{\cancel{j2}\pi t} + \frac{\cancel{j2} \sin \pi R_b (t-T_b)}{\cancel{j2}\pi (t-T_b)}
\end{aligned}$$

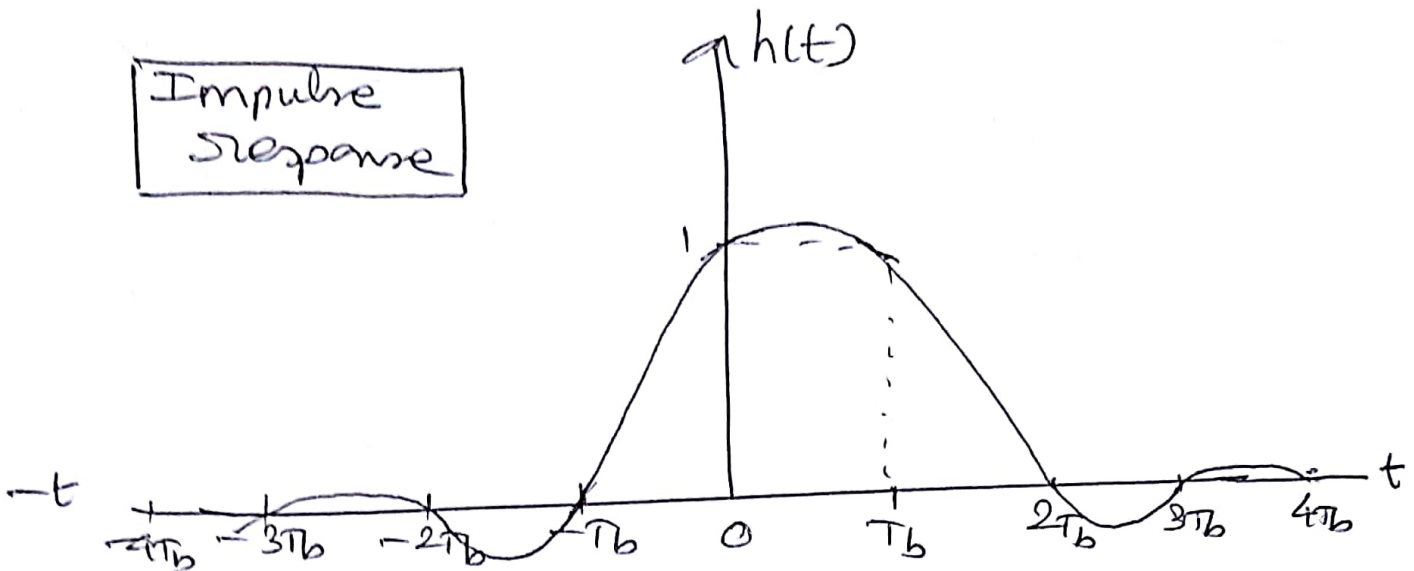
Multiply & Divide by R_b
we get

$$H(f) = R_b \frac{\sin(\pi R_b t)}{(\pi R_b t)} + \frac{R_b \cdot \sin \pi R_b (t-T_b)}{\pi R_b (t-T_b)}$$

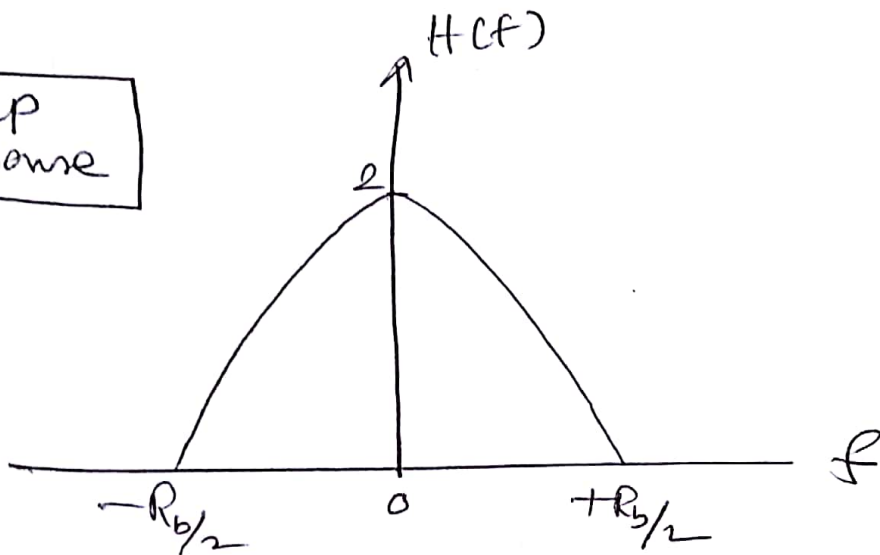
$$H(f) = R_b \cdot \text{Sinc}(R_b t) + R_b \text{Sinc } R_b (t-T_b)$$

Hence for every unit impulse applied to the input of this filter, two unit impulses spaced T_b sec apart are produced at the filter o/p.

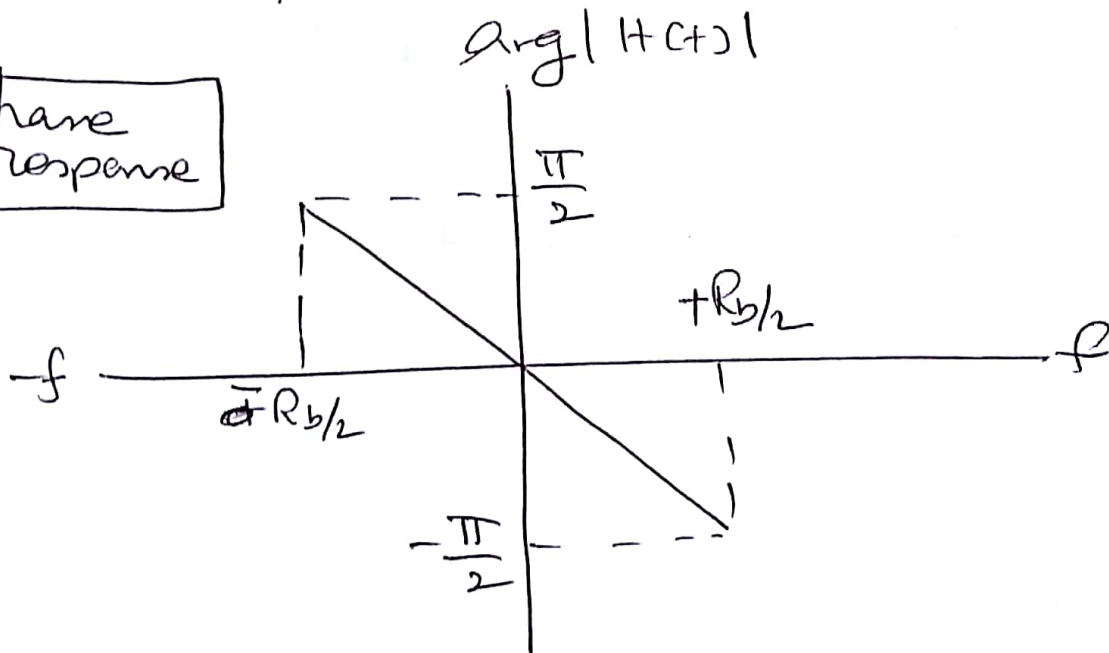
Impulse response



Amp response



Phase response



The binary data 0010110 is applied to the i/p of a duo binary system without a precoder. Construct the duo binary coder o/p and the corresponding receiver o/p without a precoder.

b_k	0	0	1	0	1	1	0
b_k in Polar form	-1	-1	+1	-1	+1	+1	-1
$C_k = b_k + b_{k-1}$ (+)	0	-2	0	0	0	+2	0
$b_k = C_k - b_{k-1}$ (+)	-1	-1	+1	-1	+1	+1	-1
	0	0	1	0	1	1	0

The binary data 001101001 is applied to the i/p of a duobinary system. Construct the duobinary codes o/p & the corresponding receiver o/p without a precoder.

(b) Suppose that due to error during transmission the level at the receiver i/p produced by the second digit is reduced to zero. Construct the new receiver o/p.

b_k	0	0	1	1	0	1	0	0	1
b_k in Polar form	$\bar{1}$	$\bar{1}$	$+1$	$+1$	-1	$+1$	-1	-1	$+1$
$c_k = b_k + b_{k-1}$ (+1)	0	-2	0	+2	0	0	0	-2	0
$b_k = c_k - b_{k-1}$ (+1)	-1	-1	+1	+1	-1	+1	-1	-1	+1
	0	0	1	1	0	1	0	0	1

(b)

c_k	0	0	0	+2	0	0	0	-2	0
$b_k = c_k - b_{k-1}$ (+1)	-1	+1	-1	+3	-3	+3	-3	+1	-1
	0	1	0	1	0	1	0	1	0

The binary data 001101001 is applied to the i/p of a duobinary system.

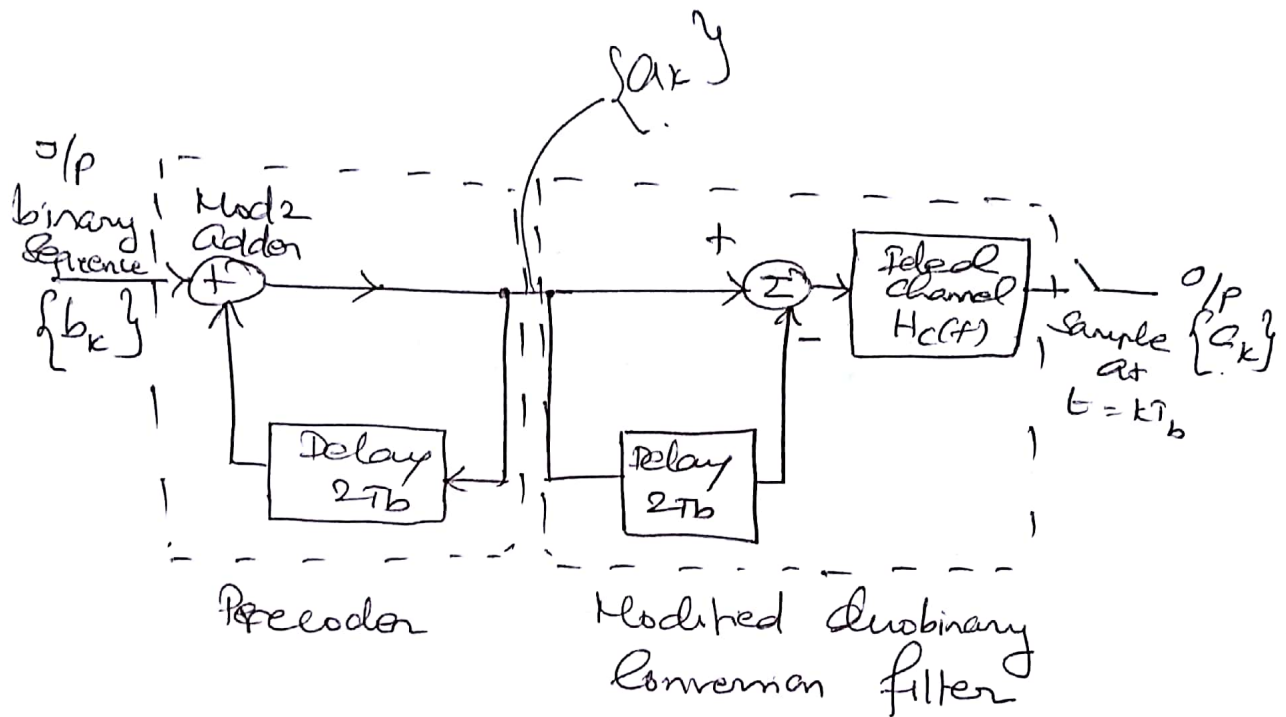
(a) Construct the duobinary coder o/p & the corresponding receiver o/p with a precoder

(b) Suppose that due to error during transmission the level at the receiver i/p produced by the second digit is reduced to zero, construct the new receiver o/p.

b_k	0	0	1	1	0	1	0	0	1
$a_k = b_k \oplus a_{k-1}$ ⁽¹⁾	1	1	0	1	1	0	0	0	1
a_k in polar form	+1	+1	-1	+1	+1	-1	-1	-1	+1
$q_k = a_k + a_{k-1}$ ⁽⁺¹⁾	+2	+2	0	0	+2	0	-2	-2	0
$ c_k $	2	2	0	0	2	0	2	2	0
b_k	0	0	1	1	0	1	0	0	1
(b) q_k	+2	0	0	0	+2	0	-2	-2	0
$ c_k $	2	0	0	0	2	0	2	2	0
b_k	0	1	1	1	0	1	0	0	1

Modified Duo binary Technique:

- involves a correlation span of two binary digits.
 - Subtracts input binary digits
- Speed $2T_b$ Sec



Let $\{b_k\}$ be the input to the Precoder, then the o/p from the precoder is given by

$$a_k = b_k \oplus a_{k-2} \text{ (Mod 2)}$$

The o/p from the ^{addition} duobinary conversion filter is given by

$$a_k = a_k - a_{k-2}$$

When a_k can take ± 1 , then

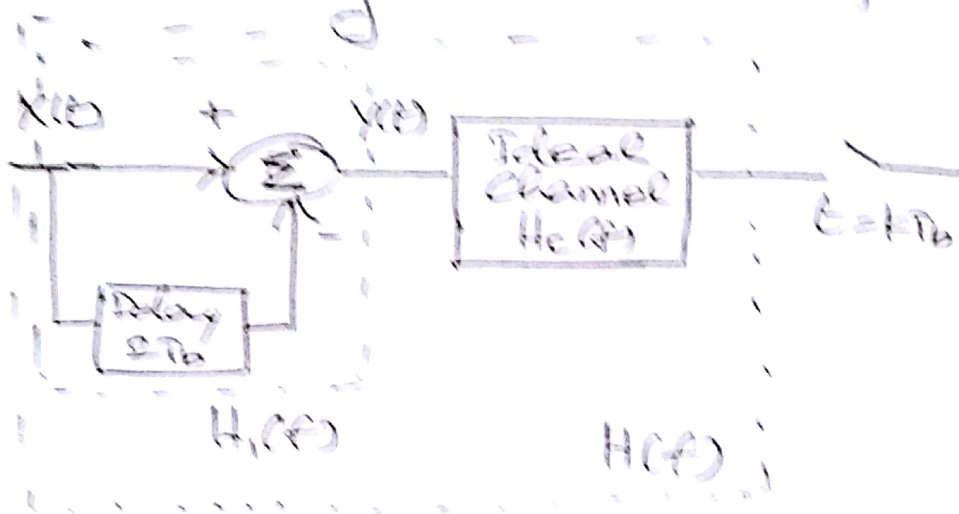
a_k can take three values

as $-2V, 0$ & $+2V$

The original frequency at O/P can be detected based on the following decision rule:

$$b_p = \begin{cases} S_{m0} & \text{if } |C_k| < 1V \\ S_{m1} & \text{if } |C_k| > 1V \end{cases}$$

Impulse response of Modified duobinary conversion filter:



Let $x(t)$ be the up to modified duobinary conversion filter and the o/p from the filter is given by $y(t) = x(t) - x(t - 2T_b)$ → (1)

Taking Fourier transform of eq (1) we get

$$Y(f) = X(f) [1 - e^{-j2\pi f(2T_b)}]$$

$$H_1(f) = \frac{Y(f)}{X(f)} = 1 - e^{-j4\pi f T_b} \rightarrow (2)$$

where $H_1(f)$ be the transfer function of the duobinary convolution filter and T_b be the bit duration.

For an ideal channel of bandwidth B_0 which is equal to $R_b/2$, the transfer function of the ideal channel is given by

$$H_c(f) = \begin{cases} 1 & |f| \leq R_b/2 \\ 0 & |f| > R_b/2 \end{cases} \rightarrow (3)$$

The overall transfer function of the system is given by

$$H(f) = H_1(f) \cdot H_c(f) \\ = (1 - e^{-j4\pi f T_b}) H_c(f) \rightarrow (4)$$

Sub. (3) in (4) we get

$$H(f) = \begin{cases} 1 - e^{-j4\pi f T_b}, & |f| \leq R_b/2 \\ 0, & \text{otherwise} \end{cases} \rightarrow (5)$$

Impulse response can be obtained by taking the inverse Fourier transform of $H(f)$ as given

$$h(t) = \int_{-\infty}^{\infty} H(f) e^{j2\pi f t} df$$

$$h(t) = \int_{-R_b/2}^{+R_b/2} (1 - e^{-4\pi f T_b}) e^{j2\pi f t} df$$

$$= \int_{-R_b/2}^{+R_b/2} e^{j2\pi f t} df - \int_{-R_b/2}^{+R_b/2} e^{j2\pi f (t - 2T_b)} df$$

$$= \left[\frac{e^{j2\pi f t}}{j2\pi t} \right]_{-R_b/2}^{+R_b/2} - \left[\frac{e^{j2\pi f (t - 2T_b)}}{j2\pi (t - T_b)} \right]_{-R_b/2}^{+R_b/2}$$

$$= \frac{e^{j2\pi \cdot \frac{R_b}{2} \cdot t} - e^{j2\pi (-\frac{R_b}{2})t}}{j2\pi t} - \left(\frac{e^{j2\pi \cdot \frac{R_b}{2} (t - 2T_b)} - e^{-j2\pi \cdot \frac{R_b}{2} (t - 2T_b)}}{j2\pi (t - T_b)} \right)$$

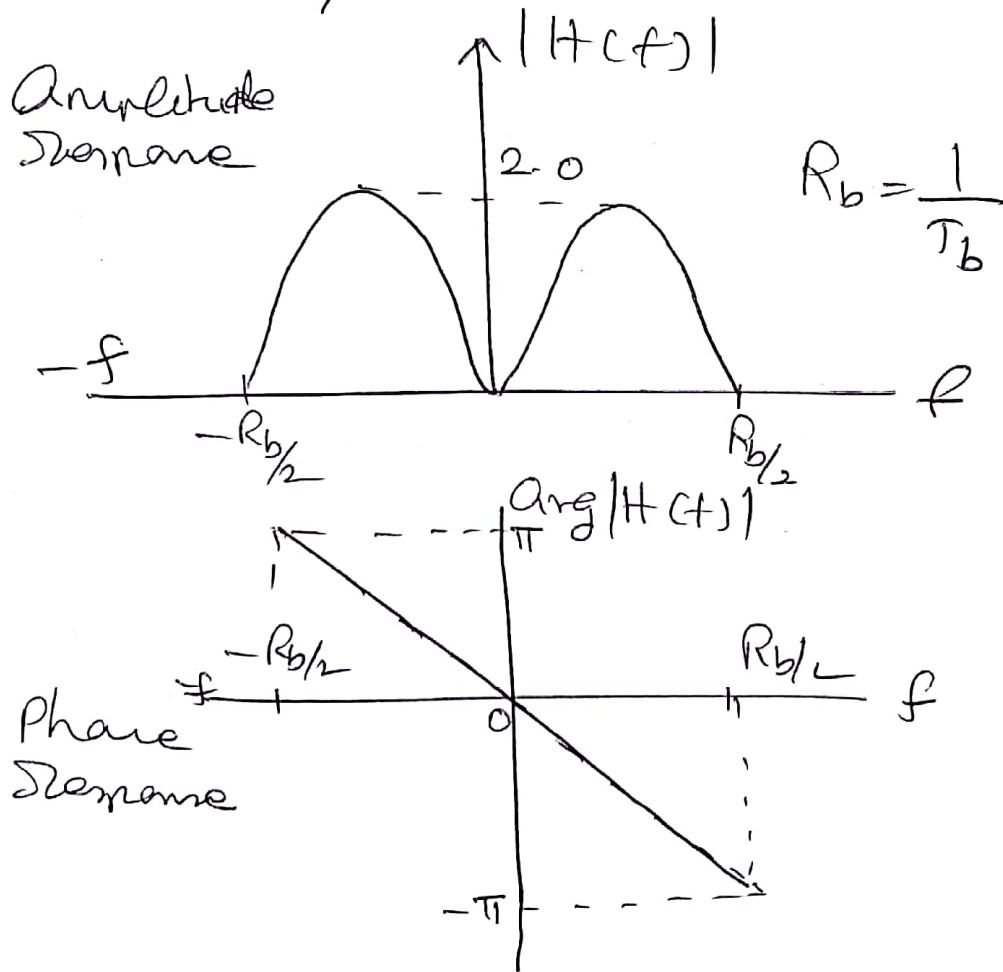
$$= \frac{j2 \sin(\pi R_b t)}{j2\pi t} - \frac{j2 \sin \pi R_b (t - 2T_b)}{j2\pi (t - 2T_b)}$$

Multiply & divide by R_b we get

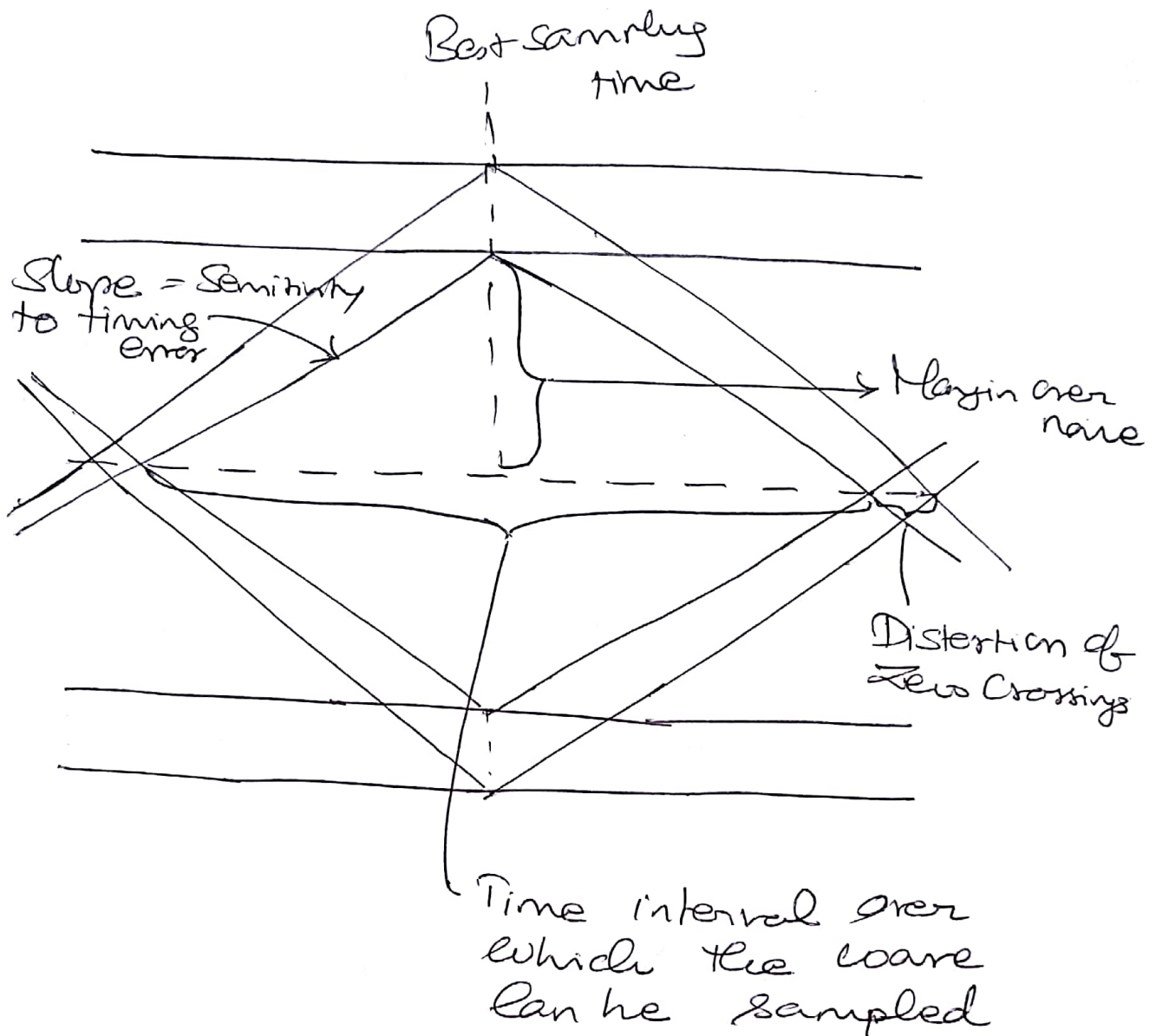
$$\begin{aligned} H(f) &= R_b \frac{\sin \pi R_b t}{\pi R_b t} - R_b \frac{\sin \pi R_b (t - 2T_b)}{\pi R_b (t - 2T_b)} \\ &= R_b \text{sinc}(R_b t) - R_b \text{sinc} R_b (t - 2T_b) \end{aligned}$$

Lee impulse response of the modified duobinary codes consists of two sine pulses that are spaced by $2T_b$ Secs.

Frequency response:



Eye Pattern:



- Used to study ISI in a PCM system
- Received wave is applied to the vertical deflection plates of an oscilloscope and a sawtooth wave is applied to horizontal deflection plates at the rate of $R = 1/T$. The resulting display is called Eye Pattern.

The interior region of eye is called Eye Opening

WIDTH of the Eye Opening:

— time interval over which the received wave can be sampled without error from ISI

HEIGHT of the Eye Opening:

— defines the noise margin at a specified sampling time

RATE of closure of eye

— defines the sensitivity of the system to timing error.

When the ISI is severe, the eye will be completely closed.

Baseband M-ary PAM Systems:

- O/p from the Pulse Generator takes on one of the M possible Amplitude Levels.

= Symbol duration

$$T = T_b \log_2 M$$

where M typically integer power of 2.

- M-ary PAM System can transmit information at a rate that is $\log_2 M$ faster than the corresponding binary PAM system.
- for a fixed bit rate, ~~the~~ the M-ary PAM requires less channel Bandwidth than a binary PAM system.
- To realize the same BER, M-ary PAM requires more Power than binary PAM system.

The binary data 011100101 are applied to the i/p of a modified duo binary system

(a) Construct the modified duo binary encoder i/p & the corresponding receiver o/p without a pre-coder

(b) Suppose that due to encoding transmission, the level produced by the 3rd digit is reduced to zero, construct the new receiver o/p

b_k	0	1	1	1	0	0	1	0	1
b_k in polar form	-1	+1	+1	+1	-1	-1	+1	-1	+1
$c_k = b_k - b_{k-2}$	-2	0	+2	0	-2	-2	+2	0	0
$b_k^a = c_k + b_{k-2}$	-1	+1	+1	+1	-1	-1	+1	-1	+1
b_k	0	1	1	1	0	0	1	0	1
c_k	-2	0	0	0	-2	-2	+2	0	0
$b_k = c_k + b_{k-2}$	-1	+1	-1	+1	-1	-1	+1	-1	+1
	0	1	0	1	0	0	1	0	1

X

The binary data 011100101 are applied to the i/p of a modified duo binary coder

(a) Construct the modified duo binary coder o/p & the corresponding receiver o/p with a precoder

(b) Suppose that due to error during transmission, the level produced by 3rd digit is reduced to zero, construct the new receiver o/p

b_k	0	1	1	1	0	0	1	0	1
$a_k = b_k \oplus a_{k-2}$	1	0	0	1	0	1	1	1	0
a_k in Polar form	+1	-1	-1	+1	-1	+1	+1	+1	-1
$c_k = a_k + a_{k-2}$	0	-2	-2	+2	0	0	+2	0	-2
$ c_k $	0	2	2	2	0	0	2	0	2
b_k	0	1	1	1	0	0	1	0	1
c_k	0	-2	0	+2	0	0	+2	0	-2
$ c_k $	0	2	0	2	0	0	2	0	2
b_k	0	1	0	1	0	0	1	0	1

X

Determine the minimum (optimum) transmission bandwidth and transmission bandwidth when the bit duration is $0.647 \mu\text{s}$

Solution: $T_b = 0.647 \mu\text{s}$

Minimum bandwidth $B = \frac{R_b}{2}$

$$= \frac{1}{2T_b}$$

$$= \frac{1}{2 \times 0.647 \mu\text{s}}$$

$$= 772 \text{ kHz}$$

Transmission BW $B = 2B_0 - f_1$

where $f_1 = (1 - \alpha) B_0$

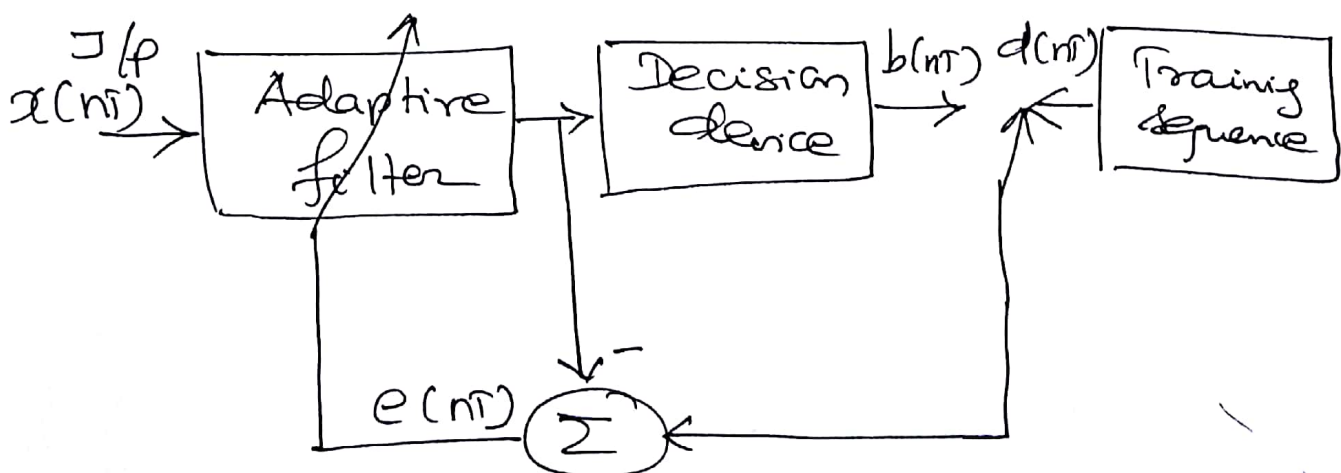
Taking $\alpha = 1$, $f_1 = 0$

$$\Rightarrow B = 2B_0 = 2 \cdot \frac{R_b}{2}$$

$$= \frac{1}{T_b}$$

$$= \frac{1}{0.647 \mu\text{s}} = 1.545 \text{ MHz}$$

Equalization:



Adaptive Equalization for data transmission:

Two basic signal processing operations to achieve high speed transmission of digital data are

- i) Discrete PAM - discrete set of possible amplitude levels to represent amplitudes of successive pulses.
- ii) Linear Modulation.

The dispersive nature of the channel leads to ISI and results in distortion. In order to realize the full transmission capacity of the channel, there is a need for adaptive equalization. Equalization refers to the process of correcting channel induced distortion.

This process is adaptive when it adjusts itself continuously during data transmission by operating on the input signal.

Two types of Equalization:

i) Prechannel Equalization:

- At the transmitter end
- Requires feedback of the channel.

ii) Post channel Equalization:

- done at the Receiver end
- done before the data transmission.

- a training sequence is transmitted through the channel so as to adjust the filter parameters to optimum values.

- Equalizer is positioned

after the receiving filter in the Receiver.

Adaptive Equalizer:

- Consists of tapped delay line filter whose coefficients are updated in accordance with the Least Mean Square (LMS)

Algorithm.

- The filter coefficients are adjusted in a step by step fashion synchronously with the incoming sequence

Two modes of operating the

Adaptive Equalizer:

i) Training period:

A known sequence is transmitted and a synchronized version of the signal is generated in the receiver where it is applied to the adaptive equalizer as the desired response.

The training sequence may be Linear Maximal Length or Pseudo Noise (PN) sequence. The length of the training sequence must be equal to or greater than that of the equalizer.

ii) Decision directed mode:

The error signal is given

$$e(nT) = b(nT) - y(nT)$$

where $y(nT)$ is the equalizer output and $b(nT)$ is the final correct estimate of the transmitted symbol $b(nT)$. An adaptive equalizer

operating in this mode is able to track relatively slow variations in channel characteristics.